Modeling and Simulation of Valve Sizing Coefficients and Cavitating Turbulent Flows in a Ball Valve*

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Abstract

Ball valve, a rotational motion valve uses ball shaped disk. It is used for on/off or throttling operations. It offers the minimum resistance to flow. To investigate the valve performance and its characteristics, the flow through the valve is studied using numerical technique. In this paper the numerical simulations were performed using commercial code FLUENT, to study the flow patterns and to estimate the valve sizing coefficient, torque coefficient and cavitation index for investigation of cavitating flows. These simulations were performed at different pressure drops and for varying percentage opening of the valve.

Key words: Ball Valve, Cavitation, Multiphase Flows, Numerical Simulation, Valve Coefficients.

1. Introduction

Ball valve is a quarter-turn valve that features a spherical closure device. As the ball move radially across the seal, the opening in the ball is exposed, which allow the flow. Ball valve is also categorized as high-pressure recovery valve. At intermediate openings, there are two throttling ports in series, one at the inlet and other at the outlet of the ball. Hence the system experiences double pressure drop, due to which ball valve has better cavitation characteristics.

Computational Fluid Dynamic (CFD) technique, are much developed and are used as an important tool in scientific research and also in industrial engineering designs. The flow pattern inside the valve, formation of vortices, and complex phenomenon like cavitation can be visualized by CFD techniques.

The commercial code, STAR-CD[TM], was used to investigate fluid flows through a ball valve and to estimate the important coefficients by Chern, et al[1]. Using FLUENT[TM], investigation of flow around a V-sector ball valve was performed by Merati, et al[2]. A three dimensional numerical analysis, was performed to reveal the velocity field, pressure distributions in a butterfly valve by using FLUENT[TM] by Huang, et al[3]. Using AVL-Fire[TM], the flow containing the bubbles in a ball valve was analyzed by van Lookeren Campagne, et al[4]. To perform three dimensional analysis, to estimate pressure drop, flow coefficient and hydrodynamic torque coefficient in a butterfly valve ANSYS

CFX[TM] was used by Song, et al[(5)]. Implementing mixture model of FLUENT[TM], the cavitating turbulent flow for two dimensional NACA0009 hydrofoil was analyzed by Bernad, et al[(6)].

In this research the main objective is to model the fluid domain of 10 inch ball valve as shown in Fig. 1, along with the prescribed length of upstream and downstream piping system. Commercial package ICEM-CFD 12.0 was used as pre-processing tool, while FLUENT 12.0 was used as solver and for post-processing. FLUENT helps to study flow thru the valve and estimate the pressure drop, volume flow rate, sizing coefficient, torque coefficient, and cavitation index.

Fig. 1 Full port ball valve

Nomenclature

C_t: Torque Coefficient
Cv: Valve sizing Coefficient (m³/hr)
CI, CI_1: Cavitation Index
D: Nominal Diameter of Ball Valve (mm)
$\vec{F}$: Body Force (N)
f : Mass Fraction
k: Turbulence Kinetic Energy (m²/s²)
n: Number of Phase
P_{sat}: Saturation Pressure (Pa)
P_{turb}: Turbulence-Induced Pressure (Pa)
Q: Volume Flow Rate (m³/s)
$S.G$: Specific Gravity
T: Hydrodynamic Torque (N-m)
u: Mean Velocity (m/s)
$\vec{v}$: Mass Averaged Velocity (m/s)
α : Volume Fraction
γ : Effective   exchange coefficient
μ : Viscosity (Kg/m-s)
ρ : Density (Kg/m³)
σ : Surface Tension Coefficient (N/m)
ΔP: Pressure Drop (Pa)

$-\overline{\rho u_i' u_j'}$: Reynolds Stress (Kg/m.s²)

2. Valve Sizing Coefficient, Torque Coefficient, and Cavitation Index

2.1 Valve Sizing Coefficient (*Cv*)

It is defined as quantity of water in US gallons at 60°F that will pass through the valve each minute with a 1 psi pressure drop across it. It is also a measure of capacity of valve, which takes account of its size and natural restriction to flow through the valve. Also it is a dimensional value. It can be calculated by following Eq. (1).

$$Cv = 1.16 \times Q \times \sqrt{\frac{S.G}{\Delta P}} \qquad (1)$$

2.2 Torque Coefficient (*Ct*)

Forces required to open/close a quarter-turn valve are caused by friction and hydrodynamic forces. Friction forces act at the valve seat and bearing surfaces. Hydrodynamic torque is caused by forces induced by the flowing fluid. Torque coefficients are dimensionless entities, varies with valve opening position. It is calculated by the following Eq. (2).

$$Ct = \frac{T}{D^3 \times \Delta P} \qquad (2)$$

2.3 Cavitation Index (*CI*)

Cavitation Index is a parameter derived from the dimensional analysis, which corresponds to the intensity of cavitation. It is defined as the ratio of forces trying to suppress cavitation to the force trying to cause it. For valves and other devices that create a pressure drop, Cavitation Index can be further defined in several ways as explained further in Fig. 2.
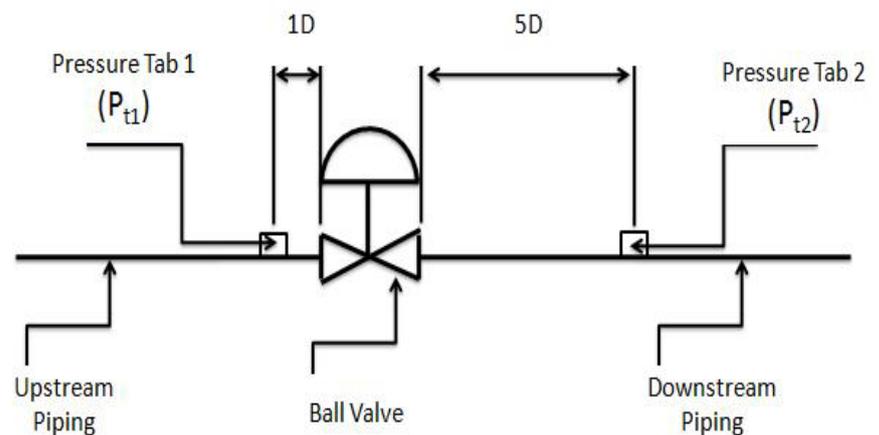

Fig. 2 Schematic diagram of ball valve and piping system

Pressure Tab 1 is installed one diameter upstream from valve. Pressure Tab 2 is installed five diameters downstream from valve. If the reference pressure in numerator is upstream pressure, P_{t1} then

$$CI = \frac{P_{t1} - P_{sat}}{\Delta P} \qquad (3)$$

If the reference pressure in numerator is downstream pressure, P_{t2} then

$$CI_1 = \frac{P_{t2} - P_{sat}}{\Delta P}$$

(4)

Equation (4) is a much preferred form over (3), since downstream pressure is the pressure closer to zone, where cavitation actually occurs. Therefore downstream pressure, more directly influences the cavitation process. Equation (3) & (4) are related by the following equation.

$$CI = CI_1 + 1$$

(5)

Table 1 Cavitation index range (*Courtesy Flowserve Corporation, USA)

Cavitation Index Range	Intensity Of Cavitation
$CI \geq 2$	No Cavitation
$1.7 < CI < 2$	No Cavitation
$1.5 < CI < 1.7$	Some Cavitaiton
$1 < CI < 1.5$	Sever Cavitation
$CI \leq 1$ or negative	Flashing

3. CFD Modeling

3.1 Model Description

For this study a 10 inch nominal diameter ball valve geometric model was initially provided in IGES format and then it was imported using ICEM-CFD 12.0. The required fluid domain was then extracted from the geometry and the prescribed length of piping system was added on upstream and downstream side. This is shown in Fig. 3.
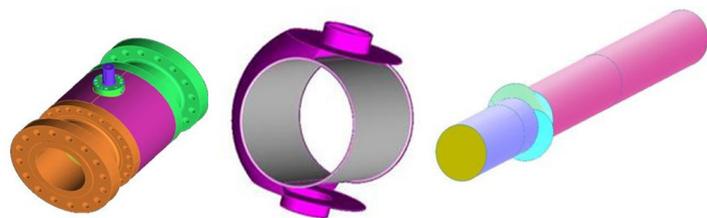

Fig. 3 Ball valve, disk (ball), and extracted fluid domain

To perform simulations at different percentage opening, different geometries were created as per angular rotation of ball valve. Tetrahedral mesh generated using ICEM-CFD 12.0, were converted to polyhedral mesh using FLUENT 12.0

3.2 Numerical Approach

3.2.1 Basic Flow Model: Working fluid is water, hence incompressible and viscous fluid, flows through the ball valve. Pressure drop between inlet and outlet being very high induces high velocity flow, hence flow studied is turbulent in nature.

3.2.2 Turbulence Model: To capture turbulence, Reynolds Averaged Navier-Stokes (RANS) equation is utilized. Its common form is written as;

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i}(\rho u_i) = 0 \tag{6}$$

$$\frac{\partial}{\partial t}(\rho u_i) + \frac{\partial}{\partial x_i}(u_i u_j) = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j}\left[\mu\left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} - \frac{2}{3}\delta_{ij}\frac{\partial u_l}{\partial x_l}\right)\right] + \frac{\partial}{\partial x_i}\left(-\rho\overline{u'_i u'_j}\right) \tag{7}$$

Where, *u* is the mean velocity and the subscript, *i, j=1~3*, refers to Reynolds-averaged components in three directions respectively. These Reynolds Stresses, $-\rho\overline{u'_i u'_j}$, must be modeled in order to close the equation. Reynolds Averaged Navier-Stokes equations modify the original unsteady Navier-Stokes equations by introducing averaged and fluctuating terms, which act like additional stresses in the fluid. These terms, called Reynolds stresses, are difficult to determine directly and so become further unknowns. The Reynolds stresses need to be modeled by additional equations of known quantities in order to achieve "closure". For this study realizable k-ε turbulence model is utilized. Standard wall function approach is utilized for the near wall treatment.

3.2.2 Cavitation Modeling:

a) *Introduction to Cavitation and Flashing:* When the internal pressure of liquid at some points falls below the vapor pressure, vapor bubbles are formed and at some point downstream, pressure rises above the vapor pressure again. As this pressure recovers, so the bubbles collapse and cavitation takes place. Flashing is a condition that occurs where pressure falls below vapor pressure and remains below it. There are then two phases flowing (liquid and its vapor) downstream. Pressure variation for cavitation and flashing process is shown in Fig. 4.

Cavitation and flashing process occurs at constant temperature and reducing pressure. Because of these processes a very large and steep density variation occurs in low pressure region.
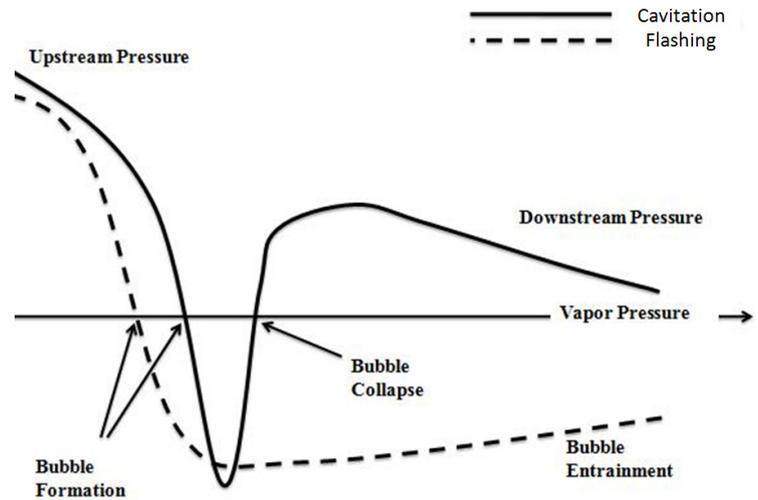
Fig. 4 Pressure Variation in cavitation and flashing process

b) ***Role of Non-Condensable Gases/Nuclei:*** The term nuclei, is other name for gas bubbles or voids in the liquid. For cavitation to occur, there must be a nuclei present. If liquid was completely deaerated (i.e. no nuclei), then liquid will sustain tension and would not cavitate when pressure dropped to vapor pressure. Liquid will cavitate far below the normal liquid vapor pressure

c) ***Cavitation Model in FLUENT:*** FLUENT's current cavitation model is available only with Mixture Model. Based on Full Cavitation Model. It accounts for all first order effects (i.e. phase change, bubble dynamics, turbulent pressure fluctuations and non-condensable gases). It provides mass transport between a single liquid and its vapor only. Cavitation model utilizes modified Rayleigh-Plesset equations for bubble dynamics and includes effects of turbulent pressure fluctuations and non-condensable gases.

d) ***Governing Equations Used for Cavitation Model:***

$$\frac{\partial}{\partial t}(\rho_m) + \nabla.(\rho_m \overrightarrow{v_m}) = 0$$

(8)

$\overrightarrow{v_m} = \sum_{k=1}^{n} \frac{\alpha_k \rho_k \overrightarrow{v_k}}{\rho_m}$ = mass averaged velocity

ρ_m = mixture density

$\alpha_k, \rho_k \ and \ \overrightarrow{v_k}$ = volume fraction, density and mass averaged velocity.

$$\frac{\partial}{\partial t}(\rho_m \vec{v}_m) + \nabla.(\rho_m \vec{v}_m \vec{v}_m) = -\nabla p + \nabla.\left[\mu_m\left(\nabla \vec{v}_m + \nabla \vec{v}_m{}^T\right)\right]$$

$$+\rho m \vec{g} + \vec{F} + \nabla\left(\sum_{k=1}^{n} \alpha_k \rho_k \overrightarrow{v_{dr,k}} \overrightarrow{v_{dr,k}}\right) \tag{9}$$

Where $\mu_m =$ Mixture viscosity

$$\mu_m = \sum_{k=1}^{n} \alpha_k \mu_k$$

$$\overrightarrow{v_{dr,k}} = \vec{v_k} - \vec{v_m}$$

Vapor Transport Equation: Working fluid is assumed to be a mixture of liquid, its vapor and non-condensable gases. Vapor transport equation governs the vapor mass fraction 'f', given by

$$\frac{\partial}{\partial t}(\rho_m f) + \nabla(\rho_m \vec{v}_v f) = \nabla(\gamma \nabla f) + R_e - R_c \tag{10}$$

Where $\rho_m =$ Mixture density,
$\vec{v}_v =$ velocity vector of vapor phase,
$\gamma =$ effective exchange coefficient,
R_e & $R_c =$ Vapor generation and condensation rate terms, derived from Rayleigh-Plesset equations and limiting bubble size consideration. These rates are functions of instantaneous local static pressure and turbulence-induced pressure. Since turbulence has significant effect on cavitating flows, the phase change threshold pressures is raised from saturation pressure to a new function which is summation of saturation pressure and turbulence-induced pressure. Equations are as follows
When $p < p_v$

$$R_e = C_e \frac{\sqrt{k}}{\sigma} \rho_l \rho_v \sqrt{\frac{2(p_v - p)}{3\rho_l}}(1 - f_v - f_g) \tag{11}$$

When $p > p_v$

$$R_c = C_c \frac{\sqrt{k}}{\sigma} \rho_l \rho_l \sqrt{\frac{2(p - p_v)}{3\rho_l}} f_v \tag{12}$$

$$p_v = \frac{1}{2}(p_{sat} + p_{turb})$$

$$p_{turb} = 0.39\rho k$$

$$\rho_m = \alpha_v \rho_v + \alpha_g \rho_g + (1 - \alpha_v - \alpha_g)\rho_l$$

Where Ce = 0.02, Cc = 0.01,
$k =$ local turbulence kinetic energy,
$\sigma =$ surface tension coefficient of the liquid,
f_v & $f_g =$ mass fraction of vapor and non-condensable gases,

p_{sat} = saturation pressure,

p_{turb} = turbulence-induced pressure,

ρ_v, ρ_g & ρ_l = density of vapor, non-condensable gases and liquid.

α_v & α_g = volume fraction of vapor and non-condensable gases.

3.3 Working Fluid, Operating Condition, and Boundary Condition:

Table 2 shows the working fluid used in analysis, the operating pressure, type of boundary conditions used, phases involved, and vaporization pressure.

Table 2 Working condition, operating and boundary conditions

For Numerical Prediction of		
	Valve sizing and Torque Coefficient	Cavitating Flow
Working Fluid	Water	Water, Water Vapor, Non-Condensable Gases
Operating Condition	101325 Pa	101325 Pa
Phases	Single Phase Flow	Two Phase Flow (Water, Water Vapor)
Vaporization Pressure		3564 Pa at 300K
Inlet Boundary Condition	Pressure Inlet Boundary Condition	Pressure Inlet Boundary Condition
Outlet Boundary Condition	Pressure Outlet Boundary Condition	Pressure Outlet Boundary Condition

4. Results and Discussion

4.1 Results of velocity field of a single phase fluid flow, Valve Sizing Coefficient, Hydrodynamic Torque and Torque Coefficient:

Following figures shows the contours of velocity on x-z plane for a pressure drops of 20.7 bar (300 psi) and different percentage opening of ball valve (10%, 30%, 50%).

0.00e+00	7.21e+00	1.44e+01	2.16e+01	2.88e+01	3.60e+01	4.33e+01	4.81e+01

Fig. 5 Velocity contour plot for 10 percent opening

0.00e+00	7.23e+00	1.45e+01	2.17e+01	2.89e+01	3.61e+01	4.34e+01	4.82e+01
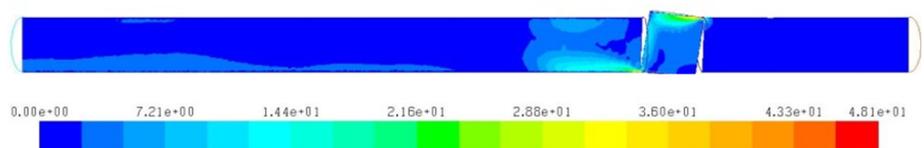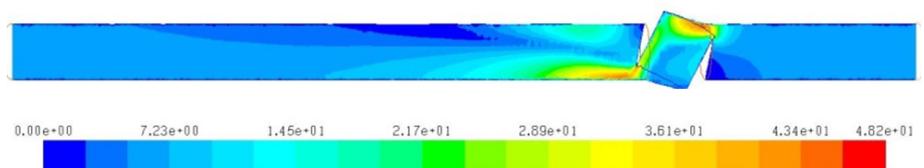
Fig. 6 Velocity contour plot for 30 percent opening
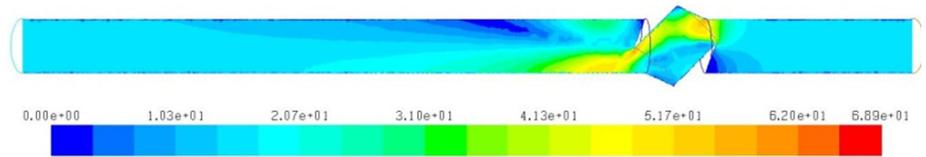
Fig. 7 Velocity contour plot for 50 percent opening

Figure 8 shows Valve Sizing Coefficient graph. The experimental value of Valve Sizing Coefficient for 100 percent opening is 3180. The value obtained from simulation result for 100 percent opening is 3086. Hence experimental Cv values and Numerically obtained values can be compared for validation. Curve characteristic signifies that Cv values depends only on geometry and are independent of flow conditions. Cv reduces as valve is closed.
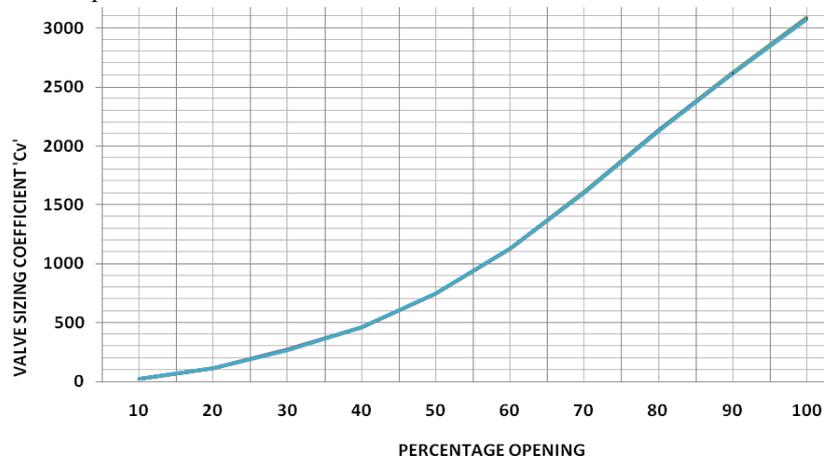

Fig. 8 Graph of variation of valve sizing coefficient

Hydrodynamic torque reduces with pressure drop. As valve is closed (i.e. reduction in percentage opening) hydrodynamic torque increases to a maximum value and then reduces. Though the hydrodynamic torque changes with pressure drop and valve opening, but in all cases, it is seen that peak point for hydrodynamic torque (maximum torque) is at 60% percent opening of valve as shown in Fig. 9.
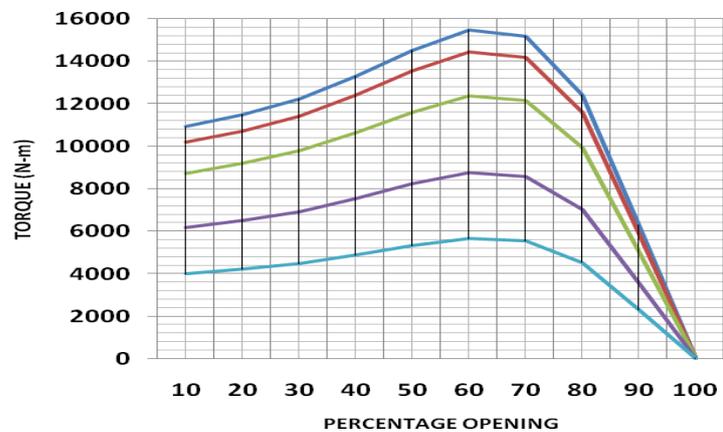
Fig. 9 Graph of variation of hydrodynamic torque at different pressure drops

Torque coefficient remains constant even as pressure varies. As valve is closed torque coefficient increases to a maximum value and then reduces. Maximum torque coefficient occurs at 80% opening for this valve as shown in Fig. 10.
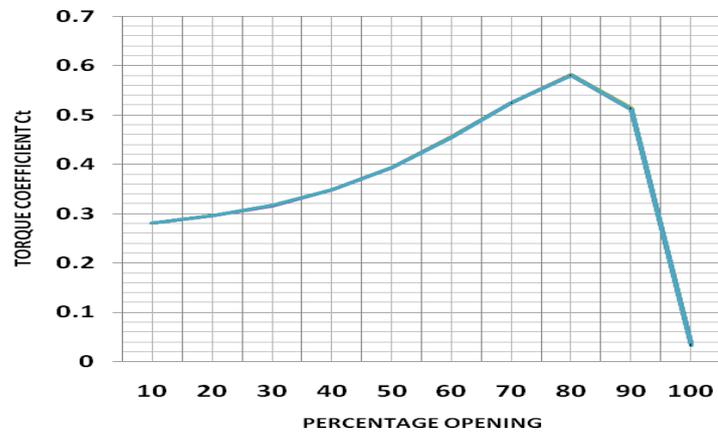
Fig. 10 Graph of variation of torque coefficient

4.2 Results pressure variation, velocity field, volume fraction of vapor and cavitation index for two phase flow:

Following figures shows the graph of absolute pressure variation along the pipe length, contour plots of volume fraction for vapor and velocity of mixture. These results are plotted for different percentage opening of ball valve (10%, 20%, 30%). Similar other simulations were performed at different pressure drops and different percentage opening of valve.

a) *Graphs of pressure variation:* The pressure variation shown in graphs is static pressure in absolute terms, caused due to variation in velocity. Double pressure drop in ball valve, one at the valve inlet and other at the valve outlet is also visible. These curves represent the occurrence of cavitation, as the local static pressure falls below vaporization pressure.
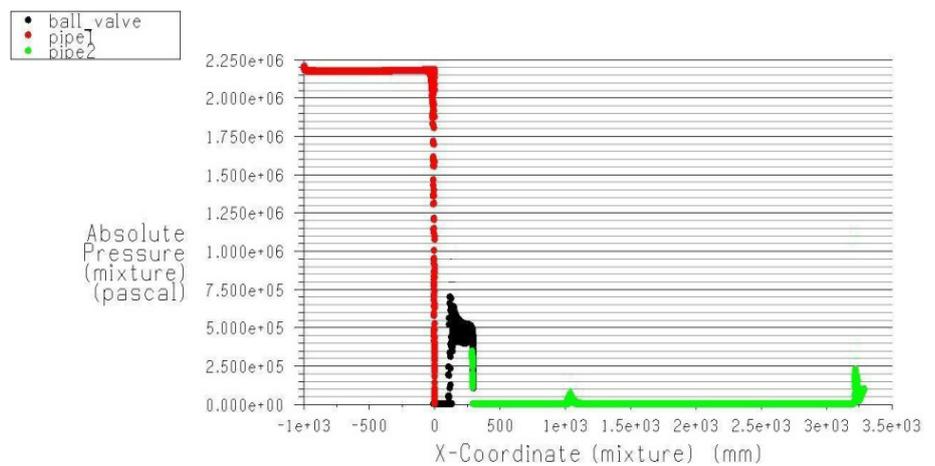
Fig. 11 Graph of absolute pressure variation for 10 percent opening
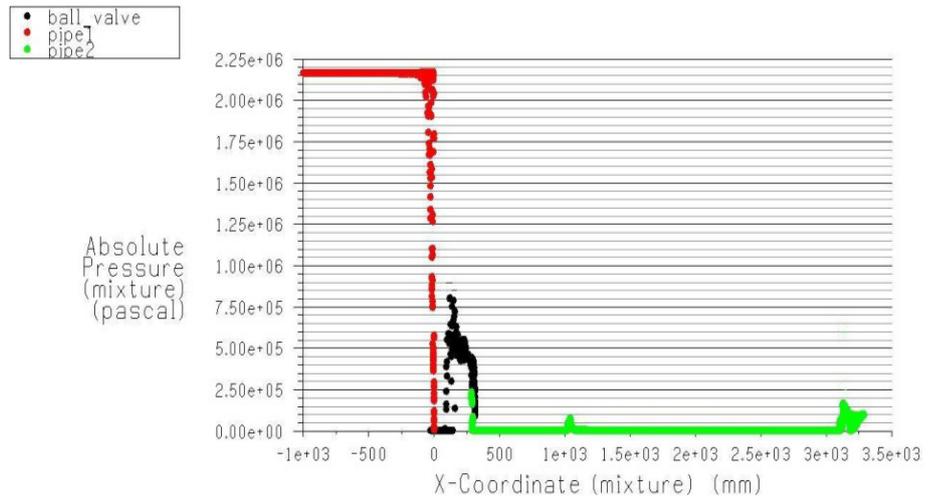
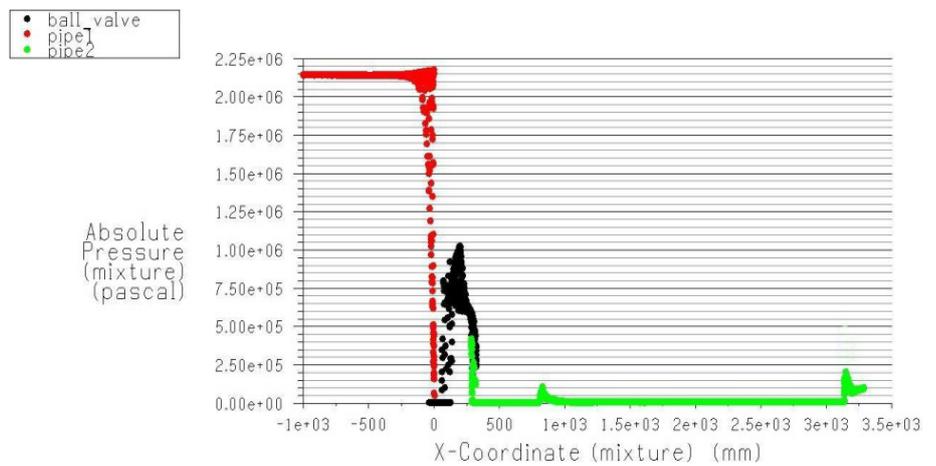Fig. 12 Graph of absolute pressure variation for 20 percent opening

Fig. 13 Graph of absolute pressure variation for 30 percent opening

b) **Velocity Contours on x-z plane:** High velocity flows causes reduction in static pressure, if pressure falls below vapor pressure than cavitation occurs. Following figures represents the velocity distribution of mixture.
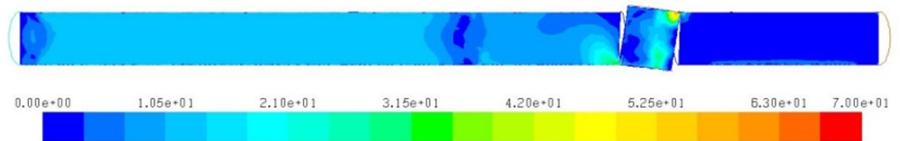

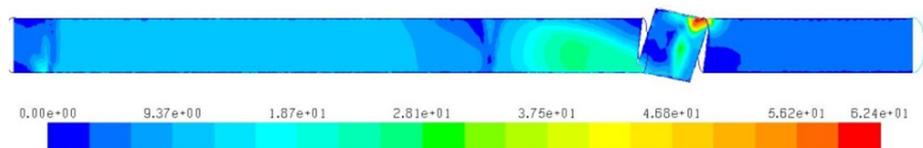Fig. 14 Mixture velocity contour plot for 10 percent opening
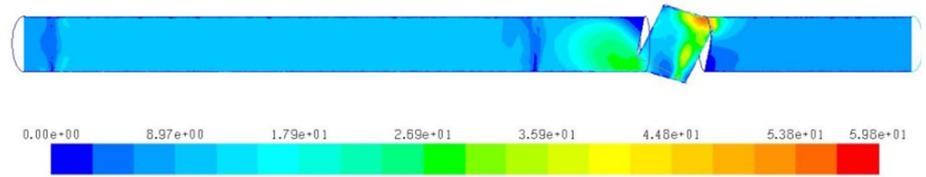

Fig. 15 Mixture velocity contour plot for 20 percent opening

Fig. 16 Mixture velocity contour plot for 30 percent opening

c) **Contour of Volume Fraction for Vapor Phase:** These contours represent the actual Cavitation or Flashing zones in the ball valve and the piping system. Also downstream piping system is severely affected by cavitating flow. Volume fraction for vapor phase varies between 0 and 1. 0 represents no vapor formation or no cavitation, whereas, 1 represents vapor flow (i.e. cavitating flow).
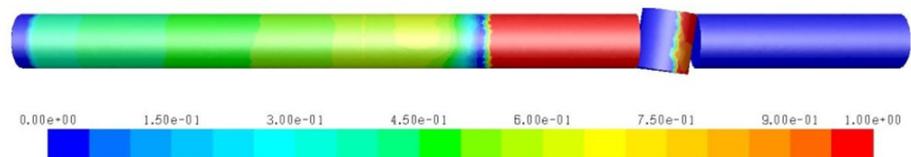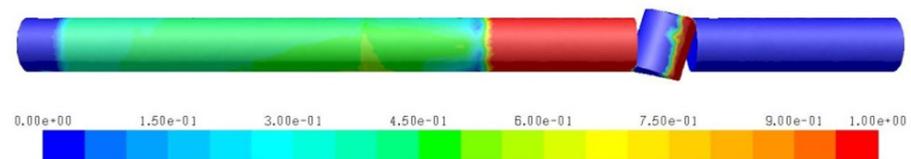

Fig. 17 Volume fraction of vapor phase for 10 percent opening

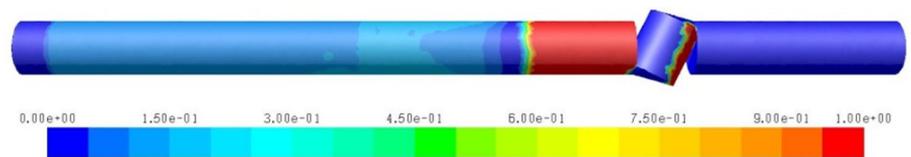Fig. 18 Volume fraction of vapor phase for 20 percent opening

Fig. 19 Volume fraction of vapor phase for 30 percent opening

d) **Results of Cavitation Index:** Cavitation Index represents the intensity of cavitation process. Following figures shows graphs for cavitation index for the downstream side of the piping system, plotted for different pressure drops and at different percentage opening.
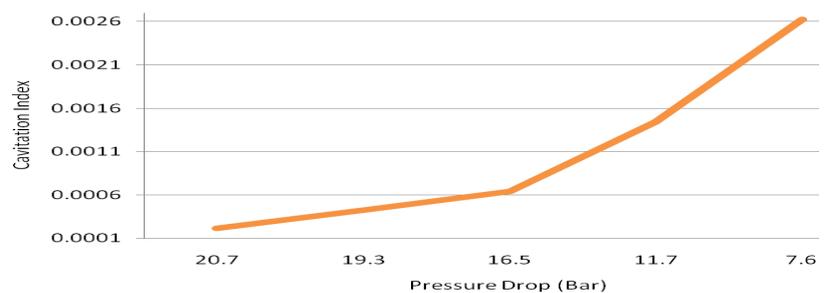

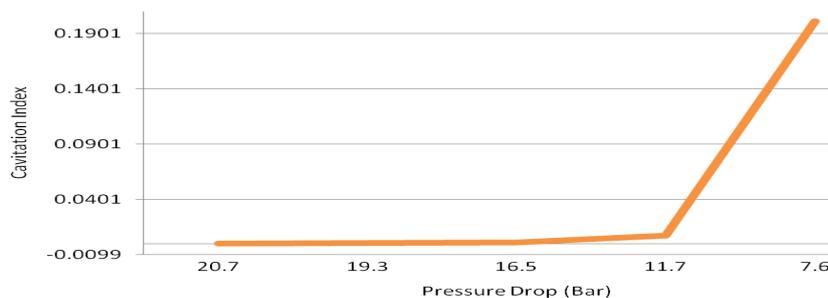Fig. 20 Cavitation index for 10 percent opening and varying pressure drop

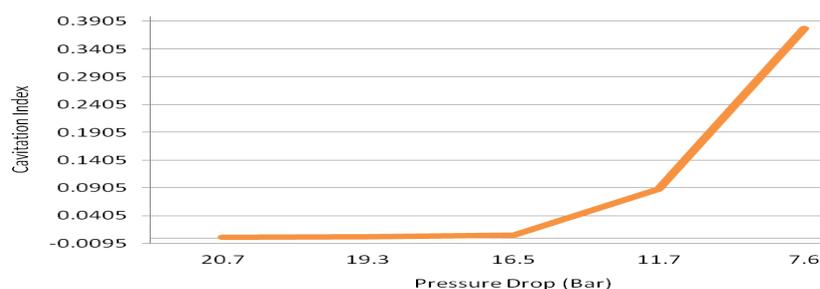Fig. 21 Cavitation index for 20 percent opening and varying pressure drop

Fig. 22 Cavitation index for 30 percent opening and varying pressure drop

These curves indicate that for a particular fixed percentage opening as the pressure drop reduces, cavitation index increases. This indicates that cavitation index depends on pressure drop. Hence, cavitation reduces as pressure drop reduces.

5. Conclusion

- As valve is closed its sizing coefficient reduces.
- Torque coefficient raises to a maximum point and then reduces, in this study it is maximum at 80 percent opening.
- Hydrodynamic torque increases to a peak point and falls as valve is closed. It is maximum at 60% opening.
- Though maximum torque coefficient is obtained at 80 percent of valve opening, it does not mean that hydrodynamic torque is maximum at the same percentage opening.
- Cavitation Index depends both on pressure drop and percentage opening.
- A high intensity cavitating turbulent flow was observed at 20.7 bar (300 psi) and 10 percent valve opening.

Acknowledgment

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